## Advanced General Relativity and Black Holes PHY 690 M

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**Course Objectives :** To cover advanced research aspects of General Relativity in a Differential Geometric setting with applications to the study of the space time geometry of black holes. The course is geared towards students intending to continue into a Ph.D thesis on General Relativity, Quantum Gravity or String Theory.

**Pre-requisites : Special and General Relativity PHY 407.** Exceptional motivation and commitment to understanding the advanced aspects of General Relativity and related issues is required.

**Evaluation:** A one semester review project with a 30 minutes Seminar and a maximum 10 page (references and title/abstract extra) report with marks 50 + 50.

**Report:** Should be in standard e-print arXiv paper format single column and references should be in standard format as in arXiv papers ( Check a paper from the arXiv ). There has to be a brief Abstract and a short Introduction with Sections. Maximum 10 pages (without references and abstract)

**Seminar:** Will be of strictly 30 minutes duration in standard PDF format. It should be professionally structured and organized ( Check Seminar files online). Avoid detailed calculations unless necessary. Highlight the Physics.

## Texts and References:

- 1. Geometry, Topology and Physics by M. Nakahara
- 2. Space Time and Geometry by Sean Caroll (also Appendix)
- 3. Gravitation and Cosmology by R M Wald (Appendix)
- 4. Large Scale Structure of Space Time by S. W. Hawking and G. F. R. Ellis
- 5. A Relativists Toolkit by Eric Poisson

**Consultation or Discussion:** Please make appointment by email sengupta@iitk.ac.in. For emergency only call my mobile number given on my website http://home.iitk.ac.in/~sengupta

**Tips:** Compulsory attendance of all classes and substantial effort towards a successful execution of the assigned one semester reading project. A well prepared and organized professional level seminar on the project and a well organized report as per specifications mentioned earlier.

## Lecture Plan : 42 Lectures

• Mappings, Functions, Vector and Tensor Spaces. Topological and Metric Spaces. (4)

• Differential Geometry: Manifolds, Tangent and Cotangent Spaces, Vectors and Tensors, Differential Forms, Derivatives and Lie Derivatives, Connections, Parallel Transport and Curvature. (8)

• Energy Momentum Tensor, Geodesic Congruences and Energy Conditions, Raychaudhuri Equations for Geodesic Congruences . (6)

- Surfaces, Extrinsic Curvature and Gauss Codazzi Equations (6)
- Lagrangian formulation and Field Equations. (3)
- Black Holes, Kruskal Diagrams and Penrose Diagrams. (3)
- Charged Reissner-Nordstrom Black Holes (6)
- •Rotating Kerr and Rotating/Charged Kerr Newman Black Holes. (6)